

1 On the propagation and modulation of electrostatic solitary waves observed 2 near the magnetopause on Cluster

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25 **Abstract.** We present the results of a study of Electrostatic Solitary Waves (ESWs) in which propagation
26 of a series of noncyclical ESWs is observed from one Cluster spacecraft to another over distances as great
27 as tens of km and time lags as great as a few tens of ms. This propagation study was conducted for
28 locations near the magnetopause on the magnetosheath side. Propagation was found primarily toward the
29 earth with speeds on the order of 1500 to 2400 km/s. The sizes of the ESWs obtained from these
30 velocities were on the order of 1 km along the magnetic field direction and several tens of km
31 perpendicular (i.e., pancake shaped). These results are consistent with measurements on single spacecraft
32 in which the ESW propagation is observed with time lags of only ~ 0.1 ms. Our results thus show the
33 stability of ESWs over time periods much greater than their own characteristic pulse durations of a few
34 100s of microseconds. We present also the results of a study of ESW modulation at the magnetopause on
35 the earthward side. We found that ESWs were modulated at ~ 1.3 Hz, consistent with a Pc1 wave which
36 was observed concurrently. During this time, tens of eV electron beams are present. We propose a
37 Buneman type instability in which the E_{\parallel} component of the Pc1 waves provides a mechanism for
38 accelerating electrons, resulting in the generation of the ESWs modulated at the Pc1 frequency.
39

40 1. Introduction

41

42 Electrostatic Solitary Waves (ESWs) have been highly studied since their first observations in the
43 data of S3-3 (Temerin et al., 1982) and with the advent in the 1990s of digital high time resolution
44 waveform receivers mounted on spacecraft (c.f., Matsumoto et al., 1994). ESWs are generally observed
45 in these waveform data as isolated pulses and as a series of cyclic or noncyclic pulses or wavepackets,
46 usually with similar amplitudes and pulse time durations. They are usually found in regions of space
47 which are turbulent or in which there are mixing of plasmas, such as in and near boundary layers and
48 along auroral field lines (Pickett et al., 2004a). Much of the past work, both observational and theoretical,
49 on ESWs and their association with electron phase space holes, has been discussed by Franz et al. (2005)
50 in the introduction to their work on the properties of small-amplitude electron phase-space holes observed

51 on the Polar spacecraft. In addition Ghosh et al. (2008) also reviewed many of the past ESW studies in
52 the introduction to their work on electron acoustic solitary waves in a magnetized plasma with application
53 to boundary layers. ESWs are almost always found in and near the magnetopause and its boundary as
54 first reported by Cattell et al. (2002) through Polar observations at the subsolar, equatorial magnetopause.
55 The ESWs in this region were reported by them to have amplitudes up to ~ 25 mV/m and velocities from
56 ~ 150 km/s to > 2000 km/s with scale sizes on the order of a kilometer (comparable to the Debye length).
57 ESWs and amplitude modulated electrostatic waves (AMEWs) were later found by Matsumoto et al.
58 (2003) to be associated with 3-dimensional reconnection using data from GEOTAIL as the spacecraft
59 skimmed along the dayside magnetopause. They showed that the ESWs and AMEWs were not random
60 noises but rather nonlinear coherent structures, possibly providing dissipation in the electron diffusion
61 region.

62
63 In the present study, we use data obtained on the Cluster spacecraft near the magnetopause
64 boundary layer (MPBL) to further our understanding of ESWs in this very dynamic region. We first
65 present data relating to the propagation of ESWs close to the magnetopause on the magnetosheath side.
66 For this study, we use the multi-spacecraft aspect of Cluster to determine ESW propagation speed and
67 size. The results of this study are presented in Section 2. We follow this in Section 3 with a study of
68 ESWs which are observed to occur in bursts modulated at a low frequency of approximately 1.3 Hz. The
69 Cluster observations presented in Sections 2 and 3 were obtained by the Wideband Data (WBD) plasma
70 wave receiver (Gurnett et al., 1997), the Spatio-Temporal Analysis of Field Fluctuations Search Coil
71 (STAFF-SC) and Spectrum Analyzer (STAFF-SA) instruments (Cornilleau-Wehrin et al., 2003), the
72 Fluxgate Magnetometer (FGM) (Balogh et al., 1997), and the WHISPER resonance sounder and wave
73 analyzer (Décréau et al., 1997). In Section 4 we discuss the significance of the observations contained in
74 Sections 2 and 3 with respect to the physical processes that are likely to be behind the generation of the
75 ESWs and their modulation. In addition for the ESW modulation event we discuss the characteristics of
76 the electrons using the PEACE data (Johnstone et al., 1997) and of the ions using the CIS data (Rème et
77 al. 2001). Finally, we summarize our results and present some basic conclusions in Section 5.

78 79 **2. Propagation of ESWs**

80
81 Prior to the launch of Cluster, spacecraft observations of the propagation of ESWs near the magnetopause
82 were constrained to a single spacecraft. The technique of observing and determining propagation
83 involved the use of interferometry. A dipole antenna, which spans the length from one probe to another
84 through the spacecraft body, is divided into two antennas with the spacecraft body acting as the end probe
85 for each of the two. An ESW is first detected by one of these two antennas. The delay between that
86 measurement and the detection of the ESW at the second antenna is then used, together with the known
87 antenna lengths, to get the propagation speed (c.f., Franz et al., 1998). The measurements are usually
88 oriented with respect to the background magnetic field to determine if the propagation was along the field
89 or at some angle off this direction. In most cases, the ESWs are seen propagating along the magnetic
90 field direction, either parallel or anti-parallel. However, the maximum distance traveled by ESWs with
91 these measurements was limited by the length of the antennas, thus being on the order of 50 m. With the
92 advent of Cluster, it was now possible to consider propagation from one spacecraft to another. There
93 have been two documented cases of ESW propagation on Cluster: 1) along auroral field lines at a distance
94 of $4.8 R_E$ on the nightside (Pickett et al., 2004b), and 2) in the dayside magnetopause boundary layer at a
95 distance of $11.9 R_E$ on the magnetosheath side (Pickett et al., 2008). The method for determination of
96 cross spacecraft propagation is a complex and time consuming process of defining the shape (time and
97 amplitude) characteristics of the ESWs, using a computer program to search for these signatures in the
98 data from each spacecraft, and then cross-correlating the ESW detections across the various spacecraft
99 using a series of irregularly spaced ESWs (see Pickett et al. (2004b; 2008) for more details on this
100 method). In Figure 1, which we have extracted from Figure 5 of Pickett et al. (2008), we show the 8 ms
101 waveforms from Cluster spacecraft 4 (SC4) as a black line with the waveforms from SC3 overlaid as a

102 green line and brought forward in time by its lag to SC4 by 22.49 ms. The agreement is quite striking and
103 shows that it is possible for ESWs to be stable over a 22 ms time span, allowing for the calculation of the
104 propagation speed and size of the ESWs similar to the method employed on one spacecraft.
105

106 Using this same method, a few other cases of propagation in the MPBL on the magnetosheath side were
107 found in the Cluster data set in the only period of time when the Cluster spacecraft were on the dayside
108 near the MPBL and the spacecraft were close enough to observe the propagation. This was the
109 approximate February through May 2002 period when the inter-spacecraft separations were on the order
110 of 100 km, with a perfect tetrahedron targeted for the northern cusp. Table 1 shows the spacecraft
111 locations and ESW propagation characteristics for the six documented cases near the MPBL. This table
112 provides, by column left to right, the following information: Date of cross spacecraft propagation
113 detection and location; time of detection; two spacecraft on which the detection was made; lag time of
114 detection of second spacecraft from the first as shown in previous column; pulse time duration of detected
115 propagating ESWs; spacecraft separation parallel to the magnetic field; spacecraft separation
116 perpendicular to the magnetic field; velocity of propagating ESWs; direction of propagation with respect
117 to the earth; ESW size parallel to the magnetic field; and ESW size perpendicular to the magnetic field.
118 Table 1 indicates that all of the ESWs except for the ones shown in Figure 1 are propagating toward the
119 earth with velocities on the order of 1300-2400 km/s and sizes parallel and perpendicular to the magnetic
120 field of 0.5-1.0 km and > than 40 km, respectively.
121

122 3. Modulation of ESWs

123
124 On March 3, 2002, around 22:00 UT the Cluster spacecraft were moving inbound toward Earth and
125 located in the magnetosheath, crossing the magnetopause into the cusp around 22:03 UT and on into the
126 magnetosphere/polar cap at about 22:57 UT based on the CIS ion and PEACE electron data. The crossing
127 of these two boundaries took place during the long recovery phase of a Co-rotating Interaction
128 Region/High Speed Stream (CIR/HSS) event. Figure 2 shows the total magnetic field magnitude, in nT,
129 obtained from the FGM measurements (panel a) and the electron density obtained from Whisper
130 measurements (panel b), both for Cluster spacecraft 3 (SC3) for the period 22:40 to 23:10 UT, thus
131 encompassing the crossing into the polar cap from the magnetopause/cusp boundary at 22:57 UT. At the
132 bottom of the figure is a listing of the spacecraft distance, R (in R_E), the magnetic local time, MLT (in
133 hours), and the magnetic latitude, MLat (in degrees).
134

135 The focus of the current study is the time period 22:51 to 22:55 UT, during which time the modulated
136 ESW bursts were detected almost continuously. In this period of time the electron density was $\sim 10 \text{ cm}^{-3}$
137 and the magnetic field strength was $\sim 144 \text{ nT}$ as seen in Figure 2. Based on these values we obtain an
138 electron plasma frequency $f_{pe} \sim 28.5 \text{ kHz}$, electron cyclotron frequency $f_{ce} \sim 4 \text{ kHz}$, proton cyclotron
139 frequency $f_{CH^+} \sim 2.2 \text{ Hz}$, He^+ cyclotron frequency, $f_{CHe^+} \sim 0.5 \text{ Hz}$, and O^+ cyclotron frequency $f_{CO^+} \sim 0.14$
140 Hz. At this time SC3 was located in the magnetopause/cusp boundary layer just prior to crossing into the
141 polar cap and magnetosphere proper at $\sim 9 R_E$, -74 degrees MLat and 14.7 hours MLT.
142

143 An example of the modulation of the ESWs observed during this period of time is shown in Figure 3.
144 Figure 3b shows wavelet analysis of the WBD waveform data using a Morlet mother wavelet, which
145 strongly resembles the ESWs pulses. The analyzed data cover an $\sim 2.4 \text{ ms}$ time interval (horizontal axis)
146 vs. frequency as inverse wavelet time scale (vertical scale) in the range 62 Hz to 10 kHz with color
147 indicating the power (intensity) of the waves in arbitrary units. We clearly see three bursts of electrostatic
148 waves roughly in the band of ~ 0.2 to 4 kHz. Note that the broad frequency, intense signatures (red color)
149 observed just before 0.4 and 2.0 s and centered at 1.4 s are artifacts of gain change ringing in the WBD
150 receiver and should be ignored. Figure 3a shows a representative 20 ms waveform taken from one of the
151 bursts observed in Figure 3b. One of the ESW pulses, of which there are four that are well defined, in this
152 example, has a pulse duration on the order of 300 microseconds and an amplitude of $\sim 0.64 \text{ mV/m}$ peak-

153 to-peak as indicated in Figure 3a. Pulses such as this make up the electrostatic bursts observed in Figure
154 3b in the band of 0.2 to 4 kHz. These ESWs occur in bursts that are modulated at ~ 1.3 Hz (3 bursts in 2.4
155 seconds) as opposed to being continuously or randomly observed throughout the 2.4 ms time interval.
156 Probably unrelated to the modulated ESWs is the presence of narrow-banded waves observed around 3.5
157 to 4.0 kHz (just below f_{ce}). Based on the sinusoidal nature of these waves observed in the WBD
158 waveforms and on STAFF-SA data analysis showing these waves to be right-hand polarized, they are
159 most likely whistler mode waves given their frequency.

160
161 Complementing these higher frequency wave observations are those of the STAFF-SC instrument
162 onboard SC3 for the period from 22:45 to 23:00 UT in Figure 4. Panel a (top) shows the total power
163 spectral density of the three components of the magnetic field. After filtering to retain the most energetic
164 part of the spectrogram, we analyzed the wave properties with the singular value decomposition (SVD)
165 method (Santolík et al., 2003) as follows. Theta (in degrees), the angle between the wave vector \mathbf{k} and
166 the magnetic field \mathbf{B} , is shown in panel b with the blue color code meaning \mathbf{k} and \mathbf{B} are parallel. The
167 sense of polarization is plotted in panel c with the blue and red colors meaning left- and right-hand
168 polarization, respectively (see equation (4) of Santolík et al. (2001)). Ellipticity is shown in panel d with
169 the blue and red colors meaning fully circular left- and right-handed waves, respectively. Panel e
170 provides the coherency of the waves. A low coherency value (Santolík and Gurnett, 2002) indicates that
171 there are random phase shifts between the two components in the polarization plane. For each panel,
172 frequency is plotted on the vertical scale, ranging from 0.5 to 3.5 Hz, and the superimposed black line is
173 the local proton cyclotron frequency.

174
175 The most striking feature observed in Figure 4, panel a, are the magnetic waves detected between 22:51
176 and 22:55 UT in the frequency range of about 1.2-1.7 Hz, which is greater than half of the local proton
177 cyclotron frequency. Their intensity is larger than the background fluctuations by only about two orders
178 of magnitude. Due to this relatively weak power and other electrostatic fluctuations, these waves are not
179 well seen in the electric field data. Nevertheless, analysis of the Poynting flux using these data together
180 with those shown in Figure 4 indicates that the energy of these waves is anti-parallel to the magnetic field
181 (not shown). Thus, these waves are propagating along the magnetic field from lower latitudes. The low
182 theta values of these waves (panel b) indicate that their transverse component is larger than that of the
183 compressive one. The sense of polarization is mainly left hand but with some right-hand excursions
184 (panel c). This observation when considered with the low absolute value of the ellipticity (panel d)
185 suggests the simultaneous presence of both left- and right-handed waves. Since the coherency level is
186 quite high (panel e), the polarization analysis can be trusted.

187
188 Given the properties of these waves and their frequency range, they are most likely EMIC waves of the
189 unstructured Pc1 type (Jacobs et al., 1964; Hayashi et al., 1981; Fraser et al., 1984). The Pc1 waves
190 observed in Figure 4 are relatively weak compared to those from a similar ESW modulation event
191 observed on March 30, 2002 near the plasmopause boundary layer (see Pickett et al., 2010). Pc1 waves
192 are expected to be present near the dayside magnetopause based on satellite and ground measurements
193 (Anderson et al., 1992;1996; Neudegg et al., 2002). Although there is still some uncertainty as to why
194 these Pc1 waves are found there, there is no question as to their presence just inside the magnetopause on
195 this date. Furthermore, although we have presented a single event of ESW modulation near the
196 magnetopause, several other events exist within the Cluster data set but no attempt has yet been made to
197 correlate these with the presence of Pc1 waves.

198 199 **4. Discussion**

200
201 The ESW pulse durations, being on the order of 500 microseconds or less as shown in Table 1, are
202 consistent with propagation speeds of electron holes measured on single spacecraft in this region (Cattell
203 et al., 2002). Their pancake shape and characteristic size, which along the magnetic field is of the order

204 of 1 km or less and across the field of tens of km, are consistent with electron holes as well (Franz et al.,
205 2000; Cattell et al., 2002). However, their characteristics are also consistent with electron acoustic
206 solitons resulting from theoretical models for cusp and magnetosheath plasmas (Ghosh et al. 2008;
207 Lakhina et al., 2009). Although we have been able to document propagation of ESWs across distances as
208 great as tens of km near the magnetopause on the magnetosheath side by correlating a series of noncyclic
209 ESW pulses across two different Cluster spacecraft, it was difficult and time-consuming to identify even
210 the few cases shown in Table 1. Part of the difficulty is related to the fact that in most regions where
211 ESWs are observed, i.e., boundary layers and turbulent regions, these regions are rich with other types of
212 waves, some of which are of higher intensity, thus making it harder to isolate a series of ESWs for cross
213 correlation analysis. Were we to cross correlate using only one isolated ESW pulse, we would have
214 numerous correlations, almost all of which would be meaningless. This is because in any one region of
215 space where ESW pulses are observed, they are usually numerous and of similar magnitudes and time
216 duration as mentioned in Section 2. Obviously, the active physical processes which generate ESWs in
217 any region of space at any given time will generate them with similar characteristics on an ongoing basis
218 unless significant changes (currents, beams, density perturbations) in the plasma are introduced to either
219 squelch those processes or change their characteristics due to those changes.

220
221 Our primary purpose in presenting results of propagation of ESWs was to demonstrate that nonlinear
222 ESWs which are generated close to the magnetopause can in fact be stable for as long as 22 ms, as
223 opposed to the relatively short time of ~ 0.1 ms observed on single spacecraft. This is a very long time
224 considering the time scales of the ESWs themselves (few 100s of microseconds). Further, we have
225 demonstrated that ESWs can propagate across great distances (tens of km), in relation to their sizes along
226 the propagation direction (1 km or less), without being disturbed by other waves and particles. This is
227 perhaps an unexpected result. However, when viewed in light of the analysis carried out by Chen et al.
228 (2005) based on Polar data (Franz et al. 2005), in which the widths and amplitudes of electron holes are
229 found to be only loosely constrained, this implies the real possibility of spontaneous generation of phase-
230 space holes in turbulent fluctuations and can play a role in transport and electrical conductivity in
231 collisionless plasma processes such as magnetic reconnection and boundary formation. It remains an
232 open problem to prove that ESWs are playing a role in these processes, but having information on the
233 propagation and stability of ESWs in these boundary regions will help shed light on that problem.

234
235 With regard to the modulation of ESWs, we have seen in Section 3 that co-located Pc1 waves at this
236 modulation frequency are certainly essential in explaining the modulation phenomenon. Since the
237 electron plasma period (few tens of microseconds) is usually of a time scale that is less than but consistent
238 with the ESWs observed in the region of space near the magnetopause (few 100s of microseconds), we
239 now look to the electron data for help in determining the generation of the ESWs that would also be
240 consistent with their modulation. Figure 5 shows a cross section of the energy distribution function from
241 the PEACE instrument which was recorded during the time of the ESW modulation bursts shown in
242 Figure 3. The color scale shows the number of counts accumulated over the time interval shown with
243 energy plotted on the vertical and horizontal axes. The magnetic field direction is up (or vertical) in this
244 figure. Here we clearly see that electron beams of a few tens of eV are observed at parallel and anti-
245 parallel to the magnetic field and at ~ 45 degrees from the anti-parallel direction. These beams are
246 persistent throughout the time of the observations of the modulated ESWs and Pc1 waves (~ 2251 to 2255
247 UT), while outside this interval the electrons are more isotropic and/or at higher energies.

248
249 The ion data obtained from the CIS instrument are also remarkable in that in the period when the
250 modulated ESW bursts are observed the direction of the ion velocity shows a direction reversal without
251 undergoing a significant change in magnitude. The direction of flow of the ~ 100 eV protons undergoes a
252 change primarily in the V_x (GSE) direction from approximately -30 km/s to $+20$ km/s with the V_θ angle
253 changing from -160 to -45 degrees and the V_ϕ from -55 to -85 degrees. It is possible that this change in
254 direction is related to the presence of the Pc1 waves, just as the electron beams are present primarily

255 during this same interval of time. It is also possible that the ion flow direction has changed in response to
256 the DC magnetic field pulse seen in Figure 2 during this 22:51-:22:55 UT time period or that it is
257 expected as the spacecraft approaches the polar cap boundary layer from the magnetopause/cusp region.
258

259 We are left with the question of how the Pc1 waves might be affecting the plasma environment close to
260 the magnetopause such that ESWs are generated in bursts at the Pc1 wave frequency and what role the
261 electrons and ions play in the generation of these ESWs. In order to answer this question, we first point
262 out one very important aspect of the Pc1 waves. These waves will have an electric field component
263 which lies along the magnetic field direction. This was previously demonstrated, for example, by
264 Tsurutani et al. (2003) using Polar data where an EMIC wave of similar frequency (~2.3 Hz, slightly
265 below the local f_{cp} of 3.05 Hz) was found to be propagating obliquely to the magnetic field in a polar cap
266 boundary layer. This region is very similar to the one discussed here for Cluster. The EMIC wave in the
267 Polar study was found to have a measurable E_{\parallel} component. This E_{\parallel} component can give rise to strong
268 electric currents (induced DC electric field). This electric field will then accelerate and beam thermal
269 electrons along the magnetic field. Their drift velocity will exceed the thermal velocity of the ions, which
270 allows the Buneman instability to take place (Omura et al., 2003). If $T_i \gg T_e$, this instability will lead to
271 formation of ESWs through the coalescence of large electrostatic potentials, while if $T_i \ll T_e$, ion
272 acoustic waves will result. In the case under study, T_i and T_e are approximately of the same order, but in
273 any case, not significantly different. In this case, the ESWs are still formed but the amount of trapped
274 electrons will be less (Omura et al. 2003) and thus the process less efficient at generating ESWs.
275

276 Lakhina et al. (2004) suggested that for the Polar observations presented by Tsurutani et al. (2003), the
277 ESWs could have been generated through the bi-stream electron instability as discussed in Omura et al.
278 (1996). The counter-streaming electron beams in this case arise through acceleration by the parallel
279 electric field components of the obliquely-propagating ion cyclotron waves as suggested by Tsurutani et
280 al. (2003). The analysis of Lakhina et al. (2004) showed that such beam modes would saturate by
281 trapping electrons, thus producing bipolar pulses and electron holes. We also look back to the GEOS
282 observations of Cornilleau-Wehrin (1981) in which wide spectrum electrostatic waves which extended
283 between the lower hybrid frequency and the ion plasma frequency were observed to be modulated at a
284 ULF frequency around the helium gyrofrequency. The ULF-associated electrostatic waves were observed
285 in the dayside region of the outer magnetosphere ($L > 6$) at all geomagnetic latitudes sampled by the
286 GEOS satellites (< 30 degrees). Although the Cluster observations are at a much higher latitude, we
287 believe that the phenomenon may be a similar one. The electrostatic waves observed by GEOS are
288 clearly observed in a frequency range (hundreds of Hz) much lower than Cluster (several kHz). In
289 addition, the waveforms were not available from which to determine whether ESW-type pulses were the
290 primary constituent of those GEOS electrostatic waves. Nonetheless, Roux et al. (1984) postulated that
291 electrons having parallel velocities that are close to the Alfvén velocity at the equator can be trapped in
292 the potential troughs of the ULF waves due to the small but finite parallel electric field developed by the
293 ULF waves in a multi-component plasma,. The trapped electrons are accelerated along the magnetic field
294 as the parallel phase velocity of the ULF waves increase as they leave the magnetic equator. They
295 suggest that the freshly detrapped electrons, which were found by Mauk and McPherron (1980) to be
296 modulated at the ULF frequency, are responsible for the ULF-modulated electrostatic waves. Thus, both
297 the ULF waves and the ULF-modulated electrostatic waves can be observed simultaneously, through their
298 connection with the accelerated electrons. It is beyond the scope of the present paper to carry out all of
299 the necessary computations and models to determine the precise mechanism by which the Cluster ESWs
300 are generated and modulated at the Pc1 wave frequency. However, as just discussed, the data support the
301 suggestion that the E_{\parallel} component of the Pc1 waves initiates the process, setting up the conditions
302 favorable for the Buneman instability to be initiated.
303

304 We would like to end our discussion of modulated ESWs by comparing our results to laboratory and
305 space-based observations of whistler mode wave packets. We begin with the ISEE-1 and ISEE-2

306 observation that whistler mode chorus emissions in the earth's outer magnetosphere on the dayside are
307 often accompanied by high-frequency bursts of electrostatic waves whose frequencies were slightly below
308 the electron plasma frequency. High time resolution measurements of these bursts reveal that at certain
309 times these bursts are modulated at the chorus frequency. Reinleitner et al. (1983) proposed a model in
310 which the electrons are free to move along the ambient magnetic field line under the influence of the
311 parallel electric field, E_{\parallel} , of the chorus waves. This electric field permits electrons to be trapped in
312 effective potential wells of the chorus wave and to be carried along with them at the chorus phase
313 velocity, thus exciting electrostatic waves via a two stream instability. A similar example on Polar in the
314 cusp turbulent boundary of electrostatic bursts modulated at a whistler mode frequency was consistent
315 with the proposed mechanism as that for the ISEE observations (Pickett et al., 2001). Both of these cases
316 are consistent with the initial instability being that of the Buneman instability as discussed by Omura et
317 al. (2003) and with a high frequency instability discussed by Lakhina et al. (2003) with regard to the
318 generation of ESWs in the polar cap boundary layer from Polar observations and which involved the E_{\parallel}
319 component of EMIC or Alfvén waves. Recent laboratory experiments in which a suprathermal electron
320 beam injection into a laboratory plasma has led to the generation of ESWs and electrostatic whistler wave
321 (EWW) packets (Lefebvre et al., 2010). The laboratory ESWs have time durations comparable to those
322 derived from various observations of ESWs in the magnetosphere (e.g., Pickett et al., 2009). Further,
323 these EWW packets have similar characteristics to those of the electrostatic bursts discussed by
324 Reinleitner et al. (1983) and Pickett et al. (2001), both of which being associated with whistler mode
325 waves. Although the Cluster-modulated ESW bursts discussed here do not appear to be associated with
326 the whistler mode waves observed during the study event, but rather with a much lower frequency Pc1
327 wave similar to the Cornilleau-Wehrin (1981) and Roux et al. (1983) events from GEOS, there is one
328 common element tying all of these events together. All appear to depend on the E_{\parallel} component of an
329 electromagnetic wave in the presence of the electrons, which allows the electrons to be accelerated
330 through the Buneman instability.

331

332 5. Summary and Conclusions

333

334 We have shown that it is possible to detect ESW propagation across distances of a few tens of km using
335 multi-spacecraft Cluster observations near the dayside magnetopause on the magnetosheath side.
336 However, very few cases were found by using cross spacecraft waveform correlation techniques carried
337 out on a computer with follow-up visual confirmation. The cases of high correlation were listed in Table 1
338 with their characteristic propagation speeds and sizes. These characteristics are similar to many electron
339 holes and electron acoustic solitons previously reported in the literature, and help to confirm that our
340 method for cross correlation is reliable. The primary conclusion we draw from this analysis is that ESWs
341 can be stable over distances as great as tens of km and for time periods on the order of 22 ms and greater
342 near the magnetopause. This is a very significant aspect of ESWs that needs to be considered when
343 developing theories for how ESWs interact with particles and waves and contribute to the bulk properties
344 of the plasmas in which they are found.

345

346 Our study of the modulation of the ESW bursts near the dayside magnetopause on the Earth side has
347 found that these bursts occur at the same frequency as a concurrently observed Pc1 wave at 1.2 – 1.7 Hz.
348 This Pc1 wave will have a measurable electric field component parallel to the magnetic field which acts
349 as an induced electric field. This induced electric field allows for the acceleration of electrons and ions
350 along the local magnetic field as the Pc1 wave propagates, setting up the necessary conditions for the
351 initiation of a Buneman type instability. This instability has been shown in previous theoretical and
352 observational work to lead to the generation of ESWs, which would be modulated at the frequency of the
353 wave that led to the initiation of the Buneman instability, i.e., the Pc1 waves for our event. Although we
354 have presented data showing all of the necessary conditions are present to lead to these conclusions, it is
355 an empirical result which needs to be investigated in more detail through theory and modeling.
356 Furthermore, the possibility that most of the modulated ESW events reported in the literature in

357 association with Pc1 waves observed in space are related to the modulated electrostatic wave bursts
358 reported in the literature in association with whistler mode waves needs to be studied further since all
359 cases seem to suggest that the E_{\parallel} component for accelerating particles is common across all these cases.
360 Finally, studying all of these events with those from the laboratory in which ESWs and EWWs are
361 produced will help us in understanding the various generation mechanisms of ESWs and where these
362 mechanisms are likely to be active in space.

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365
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475
476

477 **Figure Captions**

478
479 Figure 1: Example of ESW propagation from Cluster SC4 to SC3 where the SC3 waveforms have been
480 brought forward in time by the detected lag to SC4 (22.49 ms) and overlaid on the SC4 waveforms.
481 (Extracted from Figure 5 of Pickett et al., 2008).
482

483 Figure 2: Magnetic field strength and density measurements on Cluster 3 while the spacecraft is in the
484 magnetopause boundary layer on the earthward side.
485

486 Figure 3: (a) Example of ESWs detected on Cluster 3. (b) Wavelet spectrogram showing bursts of
487 electrostatic waves in the frequency range 0.2 -4 kHz and narrow-banded waves (probably whistler mode)
488 around 3.5 – 4.0 kHz. The electrostatic bursts are comprised of ESWs as shown by the location of the
489 waveform sample in Figure 3(a).
490

491 Figure 4: (a) Magnetic field spectral measurements in the frequency range 0.5 to 3.5 Hz showing the
492 presence of Pc1 waves around 1.2 – 1.7 Hz from 22:51 to 22:55 UT. (b) Theta angle of the k vector; (c)
493 Polarization of the waves; (d) Ellipticity of the waves; and (e) coherency of the waves, using the SVD
494 method as applied to the data plotted in panel (a).
495

496 Figure 5: Cross section of the electron energy distribution function during the ESW measurements shown
497 in Figure 3(a). Electron beams of a few tens of eV are present at parallel and antiparallel to the local
498 magnetic field, as well as at 45 degrees to magnetic field direction.

Table 1: Characteristics of ESWs obtained through cross spacecraft waveform correlations

Date (Year/Month/ Day)	Time (UT)	Cluster space- craft	Lag (ms)	Pulse Duration (ms)	$D_{B//}$ (km)	$D_{B\perp}$ (km)	Velocity (km/s)	Direction (referenced to Earth)	$L_{B//}$ (km)	$L_{B\perp}$ (km)
2002/02/19 11.84 R_E 13.53 MLT -53.9 MLat	22:20:27.90	4,3	22.5	0.60	30	40	1,334	Away	0.8	≥ 40
2002/04/03 11.79 R_E 10.85 MLT -52.5 MLat	18:00:54.54	2,1	19.5	0.30	38	95	1,947	Toward	0.6	≥ 95
2002/05/04 13.32 R_E 08.25 MLT -42.4 MLat	14:02:57.11	4,1	37.8	0.25	71	79	1,870	Toward	0.5	≥ 79
2002/05/04 13.26 R_E 08.27 MLT -42.6 MLat	14:08:06.19	3,1	15.6	0.30	37	97	2,365	Toward	0.7	≥ 97
2002/05/04 13.26 R_E 08.27 MLT -42.6 MLat	14:08:06.20	3,1	17.0	0.45	37	97	2,167	Toward	1.0	≥ 97
2002/05/04 13.26 R_E 08.27 MLT -42.6 MLat	14:08:06.23	3,1	21.4	0.37	37	97	1,724	Toward	0.6	≥ 97

2002/02/19

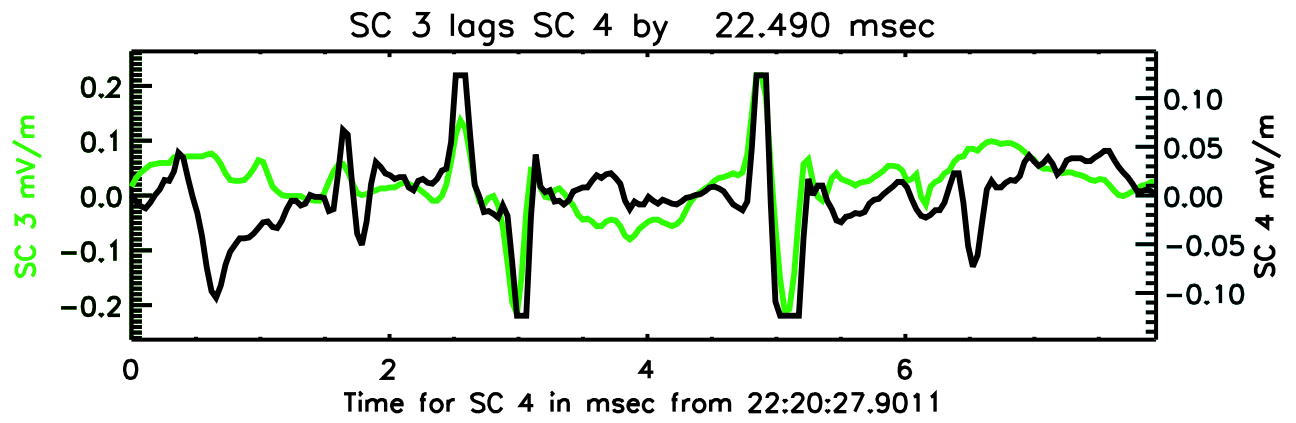


Figure 1

CLUSTER 3 - March 3, 2002

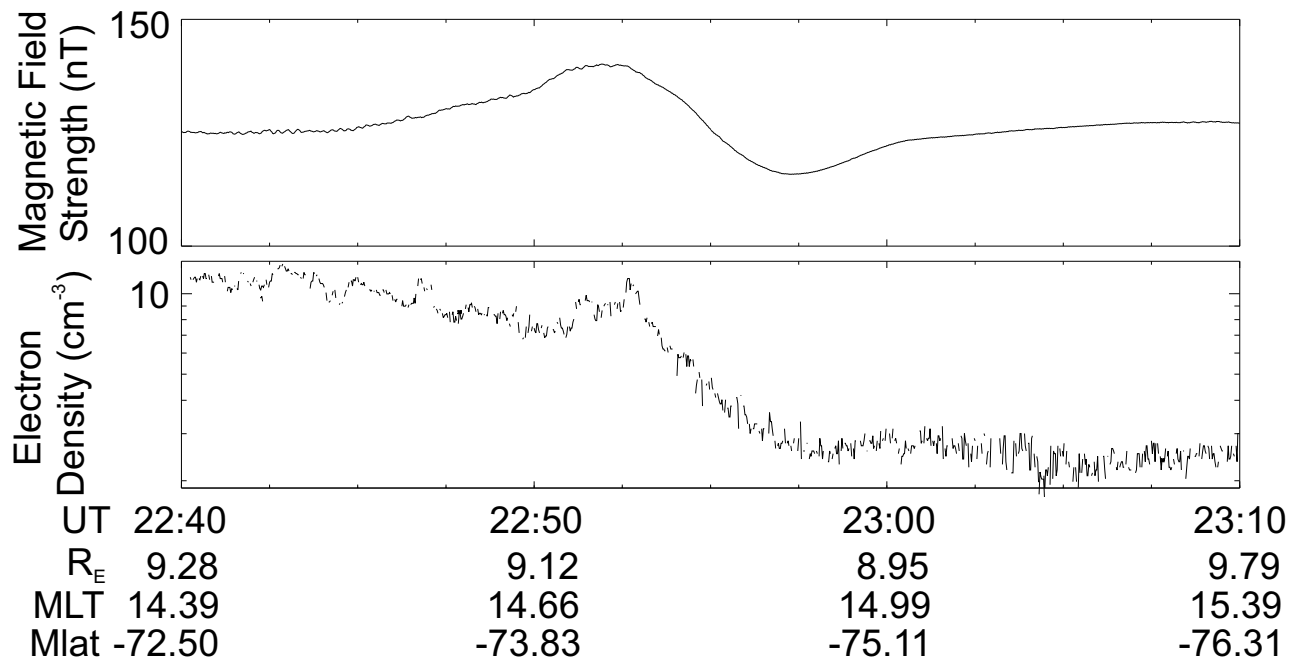
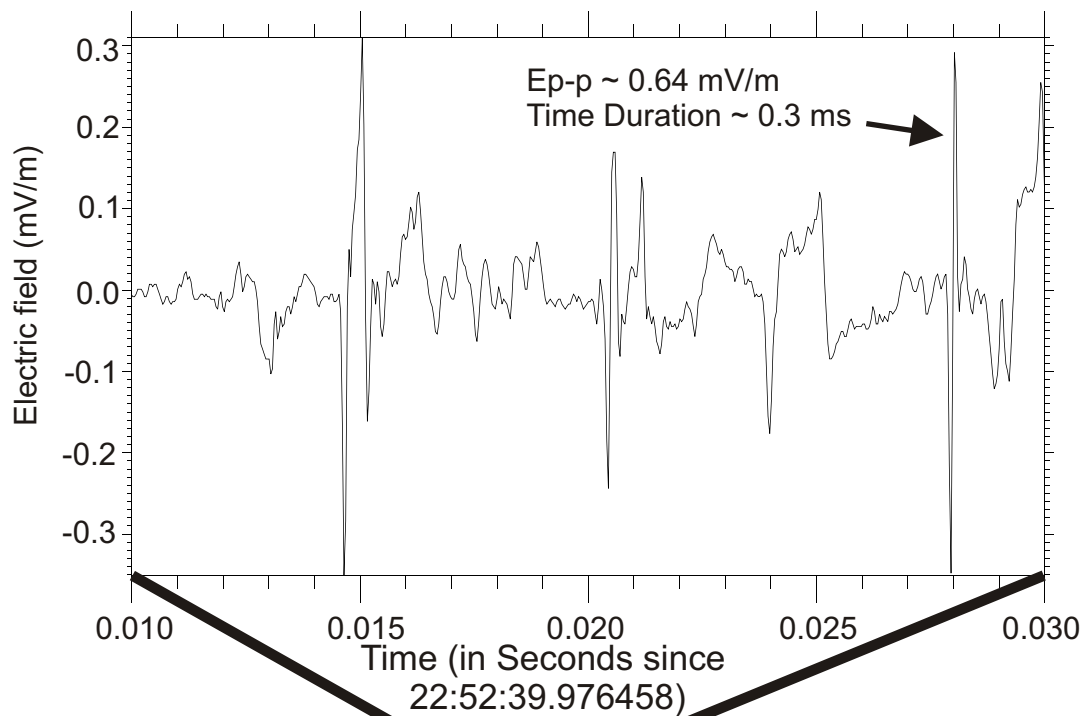


Figure 2

CLUSTER 3 - March 3, 2002

(a)



(b)

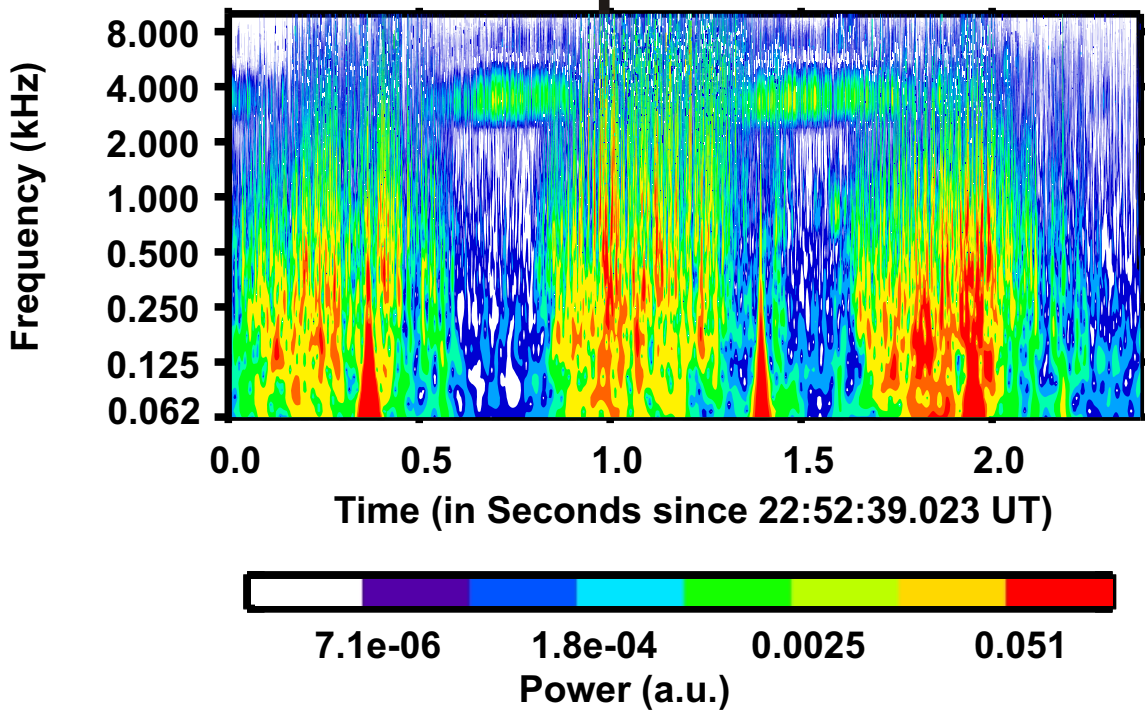


Figure 3

CLUSTER 3 - March 3, 2002

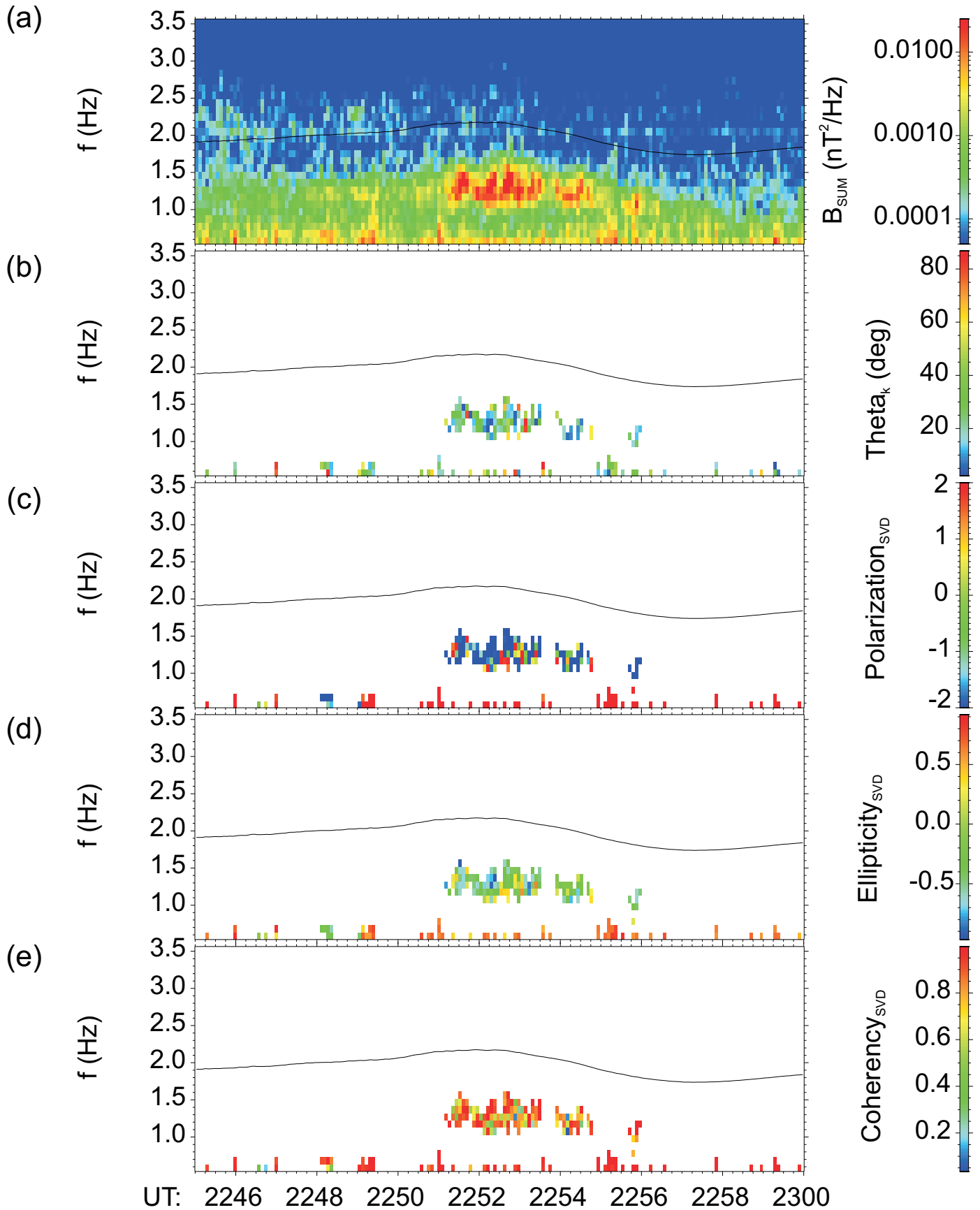


Figure 4

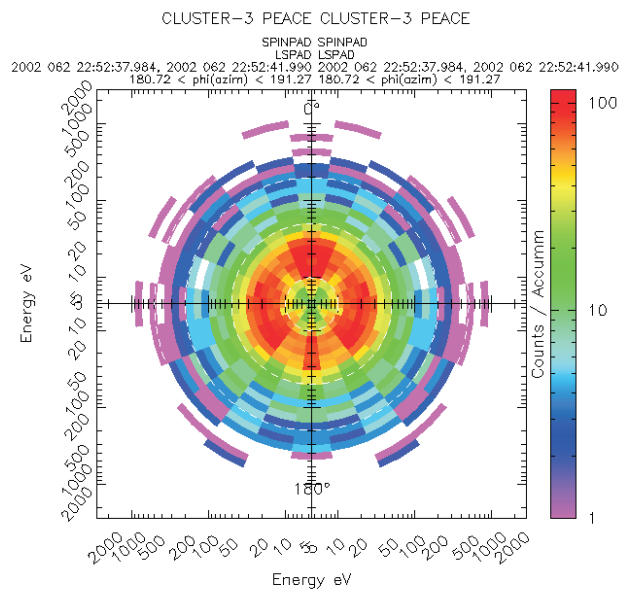


Figure 5